

# RF Front-End Implementation Challenges of In-band Full-Duplex Relay Transceivers

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19th May 2016

# Motivation

- Full-duplex (FD) technology has emerged to reach high data rates by incrementing the spectral efficiency.
- Ideal FD systems duplicate the efficiency by allowing to transmit and receive simultaneously in the same frequency band.
- Strong self-interference due to its own transmitted signal need to be mitigated.

# Motivation

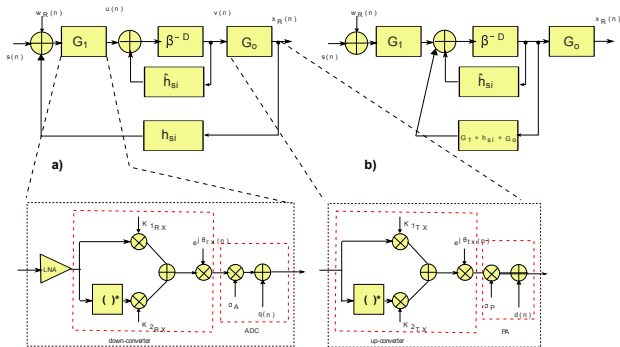
- Passive and active antenna cancellation are implemented.
- Analog RF cancellation is necessary to avoid the operation of the mixers and ADC in the saturation region.
- Digital cancellation removes the residual self-interference.
- ADC dynamic range and resolution are key aspects to define the required amount of cancellation.

# Objectives

- Transceiver hardware imperfections limit the self-interference suppression capability and affect the system performance.
- We derive an expression for the SNR at the relay output considering the effects of several RF imperfections:
  - Power amplifiers with nonlinear response
  - Phase noise and IQ imbalances from down/up-converters
  - ADC quantization noise
- The amplify-forward relay scenario is studied.

# System model

## Full-duplex relay model with RF imperfections and equivalent model



$\tilde{h}_{SI}(n) = h_{SI}(n)A_c A_{rf}$  denotes the residual SI channel after antenna and RF cancellation,  $A_c$  is the attenuation provided by antenna separation/cancellation, and  $A_{rf}$  is RF cancellation.

# RF impairments

## • LNA and ADC

The LNA gain is calculated as

$$G_L = \frac{P_{adc}}{\frac{P_{yR}}{A_c A_{rf}} + P_{soi} + PAPR}$$

- $P_{soi}$  is power of the signal of interest.
- PAPR is the peak-to-average-power ratio of the OFDM signal.

A linearized model of the ADC effects is employed.

$$x_Q(n) = \alpha_A x(n) + Q(n)$$

- $\alpha_A$  is a constant scaling factor.
- $Q(n)$  is a distortion noise term due to the quantization error.

## • Mixers: IQ imbalance and phase noise

The output of the IQ modulator can be written as

$$x_{rf}(n) = (K_{1x}x(n) + K_{2x}x^*(n))e^{j\phi_x(n)} = x_{iq}(n)e^{j\phi_x(n)}$$

- $K_{1x}$  and  $K_{2x}$  depend on the amplitude and phase mismatches in the transmitter ( $x = t$ ) or receiver ( $x = r$ )
- $\phi_x(n)$  random phase shift.

# RF impairments...

- **Mixers: Phase noise in frequency domain**

At  $k$ -th subcarrier,

$$X_{rf}(k) = \sum_{l=0}^{N-1} X_{iq}(m)\Lambda(m-k) = \Lambda(0)X_{iq}(k) + \gamma(k)$$

- $\Lambda(k) = \frac{1}{N} \sum_{m=0}^{N-1} \exp(j\phi(m)) \exp(j\frac{2\pi}{N}km)$
  - $\gamma(k)$  denotes the ICI term due to phase noise.
- **Power amplifier** A memoryless polynomial model is considered. Based on the 1-dB compression point and 3-rd and 5-th order intersection points, a polynomial model can be adjusted to model the amplifier response.

$$g[|x_{rf}(n)|] = \sum_{k=1}^{K_{pa}} c_k x_{rf}(n) |x_{rf}(n)|^{k-1}$$

where  $K_{pa}$  is the polynomial order. A linearized model is also employed to characterize the PA response. i.e.,  $\alpha_p x(n) + d(n)$ .

# Analysis of self-interference mitigation

## Derivation of equivalent feedback loop

The feedback signal

$$\begin{aligned}
 z(n) &= (G_o(n)r(n) * \tilde{h}_{si}(n)) * G_1(n) \\
 &= \alpha_a \alpha_p G_L k_{1r} k_{1t} e^{j\phi_r(n)} * \tilde{h}_{si}(n) e^{j\phi_t(n)} r(n) + \alpha_a \alpha_p G_L k_{2t} k_{1r} e^{j\phi_r(n)} * h_{si}(n) e^{j\phi_t(n)} r^*(n) \\
 &+ \alpha_a \alpha_p G_L k_{1t}^* k_{2r} e^{-j\phi_r(n)} * \tilde{h}_{si}^*(n) e^{j\phi_t(n)} r^*(n) + \alpha_a \alpha_p G_L k_{2t}^* k_{2r}^* e^{-j\phi_r(n)} * \tilde{h}_{si}^*(n) e^{j\phi_t(n)} r(n) \\
 &+ \alpha_a \alpha_p G_L (k_{1r} d(n) + k_{2r} d^*(n)) e^{j\phi_r(n)} + Q(n) \\
 &= \text{Dominant term} + \text{Residual terms}
 \end{aligned}$$

where  $r(n)$  and  $z(n)$  denote the input and output signal of the equivalent feedback channel.



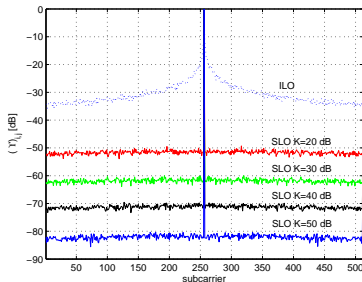
# Analysis of self-interference mitigation

Study of the dominant term in frequency domain:

$$(\mathbf{Y})_{i,j} = \sum_{k=0}^{N-1} \Lambda|N-j+k|_N \tilde{H}_{si}(k) \Lambda^* |N-i+k|_N$$

where  $|N-j+k|_N$  stands for  $(N-j+k) \bmod N$ .

- For a flat self-interference channel,  $(\mathbf{Y})_{i,j} = 0 \forall j \neq i$ , and  $(\mathbf{Y})_{i,j} = \tilde{H}_{si}(k) \forall j = i$ .
- In the case of frequency-selective channels, we verify that the ICI terms are almost negligible for moderate phase noise and considering Ricean channels with large  $K$  factor.



# Analysis of self-interference mitigation

## Estimation of self-interference channel

Considering that the channel is estimated using a set of pilots symbols defined in order to minimize the effect of RF impairments, the estimate is a noisy version of the dominant term:

$$\hat{H}_{sieq}(k) = \alpha_p G_L k_{1r} k_{1t} \tilde{H}_{si}(k) + \epsilon_H(k)$$

where  $\epsilon_H(k)$  is considered Gaussian with variance  $\sigma_\epsilon^2(k)$ .

# Signal-to-interference-plus-noise ratio at relay output

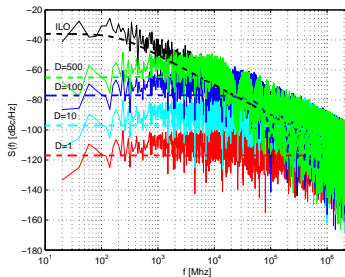
Based on the equivalent channel model and the channel estimate derived previously, we calculate the SINR at the relay output.

$$\text{SINR}_o = \frac{P_{soi}}{P_{ici} + P_{iq} + P_Q + P_{rsi} + P_{pa} + P_{feed} + P_n}$$

- Signal of interest (soi) is given by

$$\alpha_a \alpha_p \beta G_L k_{1r} k_{1t} e^{j\phi_r(n)} e^{-j\phi_r(n-D)} s(n-D)$$

Considering a single local oscillator and a short processing delay, the ICI due to phase noise can be considered negligible



# Signal-to-interference-plus-noise ratio at relay output

- $P_{pa} = \sigma_d^2$  is the power of PA nonlinear distortion.
- $P_{ici}$  is the ICI due to LO phase noise

$$P_{ici} = |\alpha_a|^2 |\alpha_p|^2 |\beta|^2 |G_L|^2 |k_{1r}|^2 |k_{1t}|^2 \sigma_\lambda^2$$

- $P_{iq}$  is the interference due to IQ imbalance

$$P_{iq} = |\alpha_a|^2 |\alpha_p|^2 |\beta|^2 |G_L|^2 (|k_{1t}|^2 |k_{2r}|^2 + |k_{2t}|^2 |k_{1r}|^2) E_s$$

- $P_Q$  is associated with the ADC quantization noise

$$P_Q = |\beta|^2 (|k_{1t}|^2 + |k_{2t}|^2) \sigma_Q^2$$

- $P_{rsi}$  is the residual self-interference due to the noisy channel estimation

$$P_{rsi} = |\beta|^2 (|k_{1t}|^2 + |k_{2t}|^2) \sigma_\epsilon^2 P_{y_R}$$

- $P_{feed}$  is the residual self-interference due to RF impairments

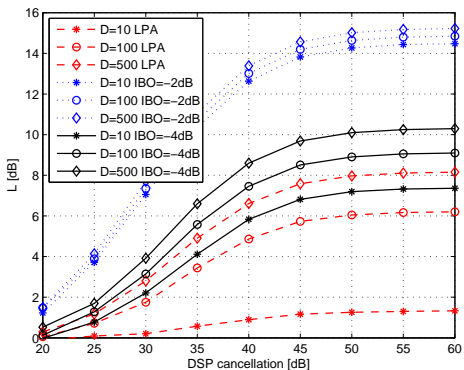
$$\begin{aligned} P_{feed} &= |\alpha_a|^2 |\beta|^2 |G_L|^2 [(|k_{1r}|^2 + |k_{2r}|^2)(|k_{1t}|^2 + |k_{2t}|^2) \sigma_d^2 + |\alpha_p|^2 (|k_{1t}|^2 |k_{2t}|^2 |k_{1r}|^2 + |k_{1t}|^2 |k_{2t}|^2 |k_{2r}|^2 \\ &+ (|k_{2t}|^2 |k_{2r}|^2 |k_{1r}|^2 + |k_{2t}|^2 |k_{1t}|^2 |k_{2r}|^2)) P_{y_R}] \sigma_w^2 \end{aligned}$$

- $P_n$  is the thermal noise at the relay output

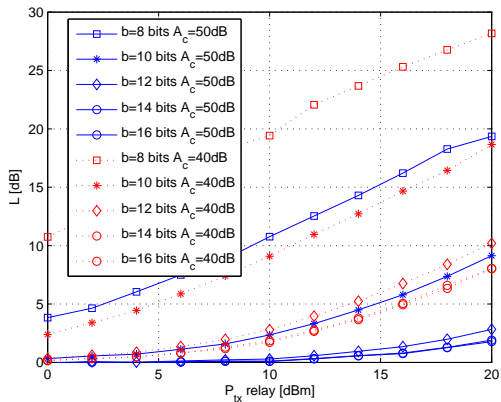
$$P_n = |\alpha_a|^2 |\beta|^2 |G_L|^2 |\alpha_p|^2 (|k_{1t}|^2 + |k_{2r}|^2) (|k_{1r}|^2 + |k_{2r}|^2) \sigma_w^2$$

# Numerical results: Nonlinear distortion and phase noise

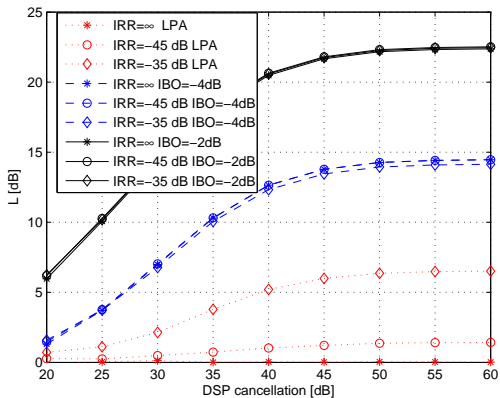
The considered figure of merit is  $L = SINR_{id} - SINR_{rf}$ . This value is useful to evaluate the performance of the relay in terms of the SI cancellation method and the robustness against the RF imperfections.



# Numerical results: Tx power and ADC resolution



# Numerical results: IQ imbalances



## Conclusion

- We derive expressions to quantify the performance of a full-duplex relay considering RF front-end impairments
- The resolution of the ADC limits considerably the system performance.
- PA nonlinear distortion need to be reduced. The linearization of the power amplifier needs to be further studied.
- A single local oscillator alleviates the phase noise problem for short processing delays.



# Thank you!

