

# Capacity Evaluation of DF Protocols for OFDMA Infrastructure Relay Links

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# Outline

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- OFDMA relay link
- Relay functionalities and protocols

## Capacity analysis

- Subcarrier pairing
- Information redistribution
- Optimization of time allocation

## Numerical evaluation

- Example setup
- Discussion

## Conclusion



# Introduction

- ▶ High data rates require dense network infrastructure while cell sites contribute substantially to the system cost
  - ▶ Two-hop communication via a relay node
- ▶ IEEE 802.16j and 3GPP LTE-Advanced air interface spec. processes
  - ▶ Which functionalities and protocols should be included?
  - ▶ Should relays operate at the physical, link, or network layer?
- ▶ Usually increased complexity and cost gives better performance
  - ▶ But severe impact on adaptive modulation and coding, scheduling, packet segmentation, signaling, handovers, etc.
  - ▶ It would be beneficial to resort to as few changes as possible in the system specification
- ▶ Our contribution: evaluating the performance of various relay functionalities under a unified analytical framework



# OFDMA relay link

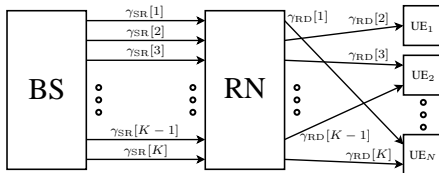


Fig. 1. Two-hop OFDMA relay link. The  $\gamma$  variables denote the subcarrier signal-to-noise ratios.

- ▶ BS–RN hop: subcarrier SNRs  $\gamma_{SR}[k] = \bar{\gamma}_{SR}[k]$ ,  $\bar{\gamma}_{SR} = \frac{1}{K} \sum_{k=1}^K \bar{\gamma}_{SR}[k]$ 
  - ▶ Static frequency-selective channel, because BS and RN are stationary
- ▶ RN–UEs hop: subcarrier SNRs  $\gamma_{RD}[l]$ ,  $f_{\gamma_{RD}[l]}(x) = (1/\bar{\gamma}_{RD})e^{-x/\bar{\gamma}_{RD}}$ 
  - ▶ Mobile users (round robin scheduling) without line-of-sight
- ▶ Time sharing factor  $\tau$  for the half-duplex time slots



# Relay functionalities and protocols

- ▶ Decode-and-forward (DF) vs. amplify-and-forward (AF)<sup>1</sup>
  - ▶ Simplest analog physical-layer repeaters omitted here
- ▶ Subcarrier pairing vs. information redistribution (only with DF)
  - ▶ Fixed vs. optimized pairing
  - ▶ Or decoding and restructuring data frames at the relay
- ▶ Buffering to overcome deep temporal channel fades
  - ▶ Possible only with DF
- ▶ Optimization of time sharing between BS–RN and RN–UE hops
  - ▶ Possible only with DF
- ▶ Different combinations of the above are of particular interest



<sup>1</sup>AF results available in [8] Riihonen *et al.* WSA 2008

# Fixed pairing without buffering

- ▶ BS–RN subcarriers are pairwise-connected with RN–UE subcarriers
  - ▶ Fixed or random mapping  $l = v[k]$
  - ▶ Relay decodes, stores and forwards without buffering

- ▶ The average capacity becomes

$$\begin{aligned} \bar{c} &= \frac{1}{K} \sum_{k=1}^K \mathcal{E} \{ \min \{ \bar{C}_{\text{SR}}[k], C_{\text{RD}}[k] \} \} \\ &= \frac{1}{K} \sum_{k=1}^K \int_0^\infty \min \left\{ \tau \log_2(1 + \bar{\gamma}_{\text{SR}}[k]), (1 - \tau) \log_2(1 + s) \right\} f_{\gamma_{\text{RD}}[k]}(s) ds \\ &= \frac{1}{K} \sum_{k=1}^K \frac{(1 - \tau) e^{\frac{1}{\bar{\gamma}_{\text{RD}}}}}{\log_e(2)} \left[ E_1 \left( \frac{1}{\bar{\gamma}_{\text{RD}}} \right) - E_1 \left( \frac{(1 + \bar{\gamma}_{\text{SR}}[k])^{\frac{\tau}{1-\tau}}}{\bar{\gamma}_{\text{RD}}} \right) \right] \end{aligned}$$

- ▶ Time sharing factor  $\tau$  can be arbitrary



# Optimized pairing without buffering

- ▶ BS–RN subcarriers are pairwise-connected with RN–UE subcarriers
  - ▶ Optimal pairing  $l = v^*[k]$  based on ordered SNRs
  - ▶ Relay decodes, stores and forwards without buffering
- ▶ From order statistics

$$f_{\gamma_{\text{RD}}[v^*[k]]}(x) = k \binom{K}{k} \sum_{l=k}^K \frac{(-1)^{l-k}}{\bar{\gamma}_{\text{RD}}} \binom{K-k}{K-l} e^{-\frac{x}{\bar{\gamma}_{\text{RD}} l}}$$

- ▶ The average capacity becomes

$$\begin{aligned} \bar{c} &= \frac{1}{K} \sum_{k=1}^K \sum_{l=k}^K (-1)^{l-k} \frac{k}{l} \binom{K}{k} \binom{K-k}{K-l} \frac{(1-\tau) e^{\frac{l}{\bar{\gamma}_{\text{RD}}}}}{\log_e(2)} \\ &\quad \times \left[ E_1\left(\frac{l}{\bar{\gamma}_{\text{RD}}}\right) - E_1\left(\frac{(1+\bar{\gamma}_{\text{SR}}[k])^{\frac{\tau}{1-\tau}}}{\bar{\gamma}_{\text{RD}}/l}\right) \right] \end{aligned}$$

- ▶ Time sharing factor  $\tau$  can be arbitrary



## Pairwise subcarriers with buffering

- ▶ BS–RN subcarriers are pairwise-connected with RN–UE subcarriers
  - ▶ Decode, store and forward
  - ▶ Infinite buffer for each subcarrier pair
- ▶ The average capacity becomes

$$\bar{c} = \frac{1}{K} \sum_{k=1}^K \min \{ \bar{c}_{\text{SR}}[k], \bar{c}_{\text{RD}}[k] \}$$

where

$$\begin{aligned} \bar{c}_{\text{RD}}[k] &= \int_0^{\infty} (1 - \tau) \log_2(1 + s) f_{\gamma_{\text{RD}}[k]}(s) ds \\ &= \frac{(1 - \tau) e^{\frac{1}{\bar{\gamma}_{\text{RD}}}} E_1\left(\frac{1}{\bar{\gamma}_{\text{RD}}}\right)}{\log_e(2)} \end{aligned}$$

- ▶ Time sharing factor  $\tau$  can be arbitrary





# Information redistribution without buffering

- ▶ Relay extracts all information from the decoded BS–RN subcarriers and then redistributes to the RN–UE subcarriers
- ▶ Average capacity is determined by the per-hop mean capacities of all subcarriers

$$\bar{c} = \mathcal{E} \{ \min \{ C_{\text{SR}}, C_{\text{RD}} \} \}$$

- ▶ BS–RN subcarriers

$$C_{\text{SR}} = \bar{c}_{\text{SR}} = \frac{1}{K} \sum_{k=1}^K C_{\text{SR}}[k] = \frac{1}{K} \sum_{k=1}^K \bar{c}_{\text{SR}}[k]$$

- ▶ RN–UE subcarriers

$$C_{\text{RD}} = \frac{1}{K} \sum_{k=1}^K C_{\text{RD}}[k], \quad \bar{c}_{\text{RD}} = \mathcal{E} \{ C_{\text{RD}} \} = \frac{1}{K} \sum_{k=1}^K \bar{c}_{\text{RD}}[k] = \bar{c}_{\text{RD}}[k]$$

- ▶ Approximation using the central limit theorem
- ▶ Time sharing factor  $\tau$  can be arbitrary



# Information redistribution with buffering

- ▶ Relay extracts all information from the decoded BS–RN subcarriers and then redistributes to the RN–UE subcarriers
  - ▶ Buffering compensates for the fading on the RN–UE hop
  - ▶ Complete restructuring of data frames over both time and frequency
- ▶ Average capacity becomes simply

$$\bar{C} = \min \{ \bar{C}_{\text{SR}}, \bar{C}_{\text{RD}} \}$$

- ▶ Time sharing factor  $\tau$  can still be arbitrary



# Optimization of time allocation

- ▶ All of the derived capacity expressions depend on the time shares  $\tau$  and  $1 - \tau$  of the respective BS–RN and RN–UE hops
- ▶ Optimization problem can be expressed as

$$\tau^* = \arg \max_{\tau} \bar{C} \text{ subject to } 0 \leq \tau \leq 1$$

- ▶ We resort to numerical optimization
- ▶ Analytical closed-form expression only for information redistribution with buffering

$$\tau^* = \frac{e^{\frac{1}{\bar{\gamma}_{RD}}} E_1\left(\frac{1}{\bar{\gamma}_{RD}}\right)}{\frac{1}{K} \sum_{k=1}^K \log_e(1 + \bar{\gamma}_{SR}[k]) + e^{\frac{1}{\bar{\gamma}_{RD}}} E_1\left(\frac{1}{\bar{\gamma}_{RD}}\right)}$$



## Example setup

- ▶ For the BS–RN channel we adopt the B5f non-line-of-sight (NLOS) rooftop-to-below rooftop channel model from the WINNER project:

TABLE I  
 POWER-DELAY PROFILE FOR THE BS–RN LINK

B5f-NLOS rooftop-to-below rooftop					
Delay [ns]	0	10	20	50	90
Power [dB]	-0.1	-5.3	-11.5	-8.9	0.0
Delay [ns]	95	100	180	205	260
Power [dB]	-5.2	-12.7	-3.5	-6.3	-4.6

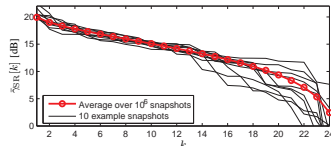
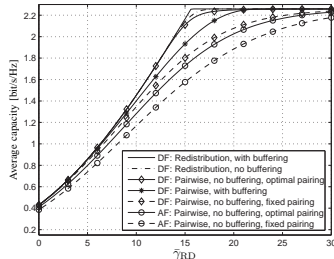


Fig. 2. The sorted BS–RN subcarrier SNRs from WINNER B5f-NLOS rooftop-to-below rooftop channel model when  $K = 24$  and  $\bar{\gamma}_{\text{SR}} = 15\text{dB}$ . The average channel is used in numerical performance evaluation.

- ▶ Implementation with subcarrier chunks, i.e., resource blocks (RBs)
  - ▶ 3GPP Release 7 baseline proposal: 375kHz RBs (25 consecutive subcarriers for 6 or 7 consecutive OFDM symbols), system bandwidth 10MHz, 600 occupied subcarriers
  - ▶ Thus,  $K = 24$



# Comparison with equal time sharing



(a) With equal time sharing ( $\tau = \frac{1}{2}$ )

Fig. 4. The average end-to-end capacities of the proposed protocols in terms of the average second hop SNR when  $\bar{\gamma}_{\text{SR}} = 15\text{dB}$ .

- ▶ Complex functionalities improve capacity but differences are small
  - ▶ DF protocol with optimized subcarrier pairing seems to offer a good trade-off between complexity and capacity
  - ▶ Benefit of buffering is comparatively small
  - ▶ AF protocols are simple but have lowest capacity



# Optimization of time sharing

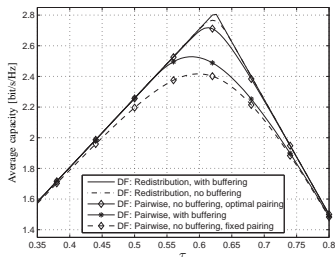
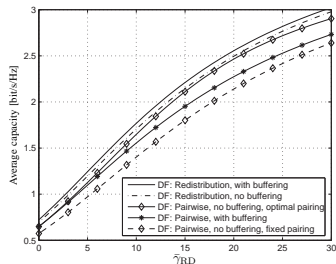


Fig. 3. Optimization of time sharing when  $\bar{\gamma}_{SR} = 15\text{dB}$  and  $\bar{\gamma}_{RD} = 25\text{dB}$ .

- ▶ The optimal value of  $\tau$  is quite the same for all considered protocols
- ▶ 50%/50% time sharing is reasonably good



# Comparison with optimized time sharing



(b) With optimized time sharing ( $\tau = \tau^*$ )

Fig. 4. The average end-to-end capacities of the proposed protocols in terms of the average second hop SNR when  $\tilde{\gamma}_{SR} = 15\text{dB}$ .

- ▶ Optimal time sharing is beneficial when the hops are unbalanced
  - ▶ In general, the weakest hop limits the performance



# Conclusion

- ▶ Analysis of the performance of OFDMA decode-and-forward relays
  - ▶ New closed-form expressions for average end-to-end capacities
- ▶ Various relaying protocols were proposed
  - ▶ Different sets of functionalities implemented in the relay
  - ▶ A common framework to allow comparison
- ▶ Useful information for specifying new systems
  - ▶ Evaluation and comparison of the performance gains due to the functionalities that can be employed only at the expense of increased complexity and cost of the network architecture
- ▶ Power allocation not considered — a future research topic (?)





# Thank you!

- ▶ Questions?
- ▶ Discussion?

